

# Glass Fibre Insulated with self-Compacting Concrete

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**Abstract:** This project describes fiber glass insulation using self-compacting concrete. Self-compacting concrete Is a high-performance concrete that flows under its own weight to completely fill the form work and self-compact without mechanical vibration. In general, concrete has strong compressive strength and weak tensile strength. In this study for increasing the tensile strength of concrete, glass fibers were added in an amount of 1kg perm 3 of concrete. Various applications of fiber glass demonstrated in research, experimental test results show the great potential of fiber glass as an alternative building material to improve the durability of materials. This is a new generation of fiber glass aimed at improving processes

**Key Word:** Tremendous potential, Imperable Material, Durability, Tensional property, Self consolidates.

## INTRODUCTION

### Self compacting concrete

In recent development in the construction industry, involves manufacture cretes day by day. Among that Self-compacting concrete plays an major role in recent days. Because of its high strength, low labor requirements, ease to handle, transport and place increased durability, and pollution control. Due to poor homogeneity of poured concrete due to poor compaction or segregation can significantly reduce the on-site performance of mature concrete. SCC is designed to facilitate proper compaction and placement of concrete in heavily reinforced structures and restricted areas. The high flow ability and high segregation resistance of SCC are achieved by:

A larger quantity of fine particles, i.e., a limited coarse aggregate content.

1. With a lower w/c ratio
2. Utilization of plasticizer.

SCC consists of the same components as conventional vibratory ordinary concrete: cement, aggregates, water, additives, and admixtures. However, a large amount of super plasticizer to lower the yield point and improve work ability, a higher percentage of powder used as a "lubricant" for coarse aggregates, and a thickener to increase the viscosity of concrete should be considered. Figure 2.1 shows the basic principle of SCC manufacturing.

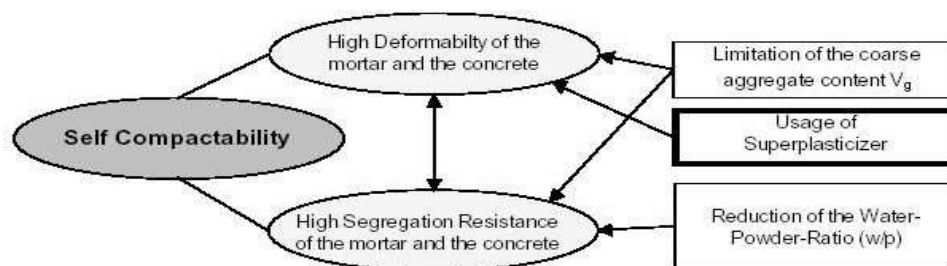


Figure 2.1 production of SCC

The following methods is already implemented to achieve self-compression of SCC.

1. Aggregate content Is Limited To (50% Coarse aggregate of concrete volume and 40% Sand of mortar volume),
2. Lower water/Cement ratio and
3. Application Of high-Dose super plasticizer

The ability of the SCC to flow under its own weight into all voids in the formwork. Tests such as Slump Flow, V-Funnel, etc. are used to determine the filling capacity of ready-mixed concrete.

- Passability: The ability of the SCC to move through narrow openings under its own weight. B. Space between flowing rebars.
- Passing eligibility can be determined using the U-Box, L-Box, Fill-Box, and J-Ring test methods.
- Separation Tolerance: The SCC must meet fill ability and pass ability with uniform composition throughout the transportation and placement process.

### Scope and objectives

The primary aim of our project is to develop Self Compacting Concrete with Glass Fibre and to study their work ability & strength characteristics.

### II.LITERATURE REVIEW

Proper compaction is necessary to achieve an acceptable concrete structure for complete packing of the mixture and even distribution with minimal segregation. His one solution to obtaining acceptable concrete structures regardless of construction quality is the use of SCC. SCC eliminates the need for internal or External vibrations, thus reducing labor and noise pollution.

Sesha dri Sekhar. T, Dr.Srinivasa Rao. P, February(2008), "Strength Properties of Glass Fiber Self-Compacting Concrete" Vol.

Experimental studies on the characteristics of Suresh Babu.T & Rama Seshuc.D,(2008),"Mechanical Properties of Self Compacting Concrete with and without Glass Fibers".

"Asian Journal of Civil Engineering", Vol. Describes the experimental work on the development of fiber glass SCC and the study of its properties. They concluded that incorporation of 0.03% glass fiber, or 600g/m<sup>3</sup> of concrete, increased strength by 2.0 to 5.5% in compression, 3.0 to 7.0% intension, and 11.0 to 20.0% in bending after 28 days.

### III.MATERIAL AND METHODS



#### Details of investigation

##### Raw Materials Used in work

Cement	-Ordinary Portland cement of 53 grade
Coarse Aggregate	-Aggregate of size 12.5 mm passing
Super plastizer	- Mineral admixtures-Flyash Chemical admixtures
Glass Fibers	- Conplast SP230
Water	-anti-crack glass fibers
	-Ordinary Potable water

##### Cement

OPC of 53 grade confirming to IS-12269 with specific gravity of 2.88.

##### Fine Aggregates

River sand confirming to IS-383 zone II with specific gravity of 2.66.

##### Coarse Aggregate

Crushed granite angular aggregate of size 12.5mm passing confirming to IS-383 having specific gravity 2.88. Chemical admixtures:

##### Super plasticizer

Super plasticizers are essential for SCC. Poly carboxylated ether-based super plasticizer—Conplast SP230 is used. The super plasticizer is required

- To provide work ability
- To reduce W/C ratio
- To increase flow ability—High slump

- To reduce Bleeding

### Glass Fibers

Cem-FIL anti-crack high dispersion glass fiber were used, Properties of Glass fiber used

- Length 12mm
- Diameter 14micron
- Specific Gravity 2.6
- No of fibers 212 million/kg

The addition of Glass fibers in SCC can improve

- Ductility
- Post crack resistance
- Energy absorption capacity
- Bleeding resistance

## IV.RESULT

### Preliminary Tests

#### Tests Forcement

##### 4.1.A. Specific Gravity Test

S.No	Description	T-I	T - II	T - III
1.	Wtof empty bottle (W1)(g)	26.8	26.8	26.8
2.	W to f bottle+water(W2)(g)	75	75	75
3.	W tofbottle+Kerosene(W3)(g)	65.5	65.5	65.5
4.	W tof bottle+Cement+Kerosene(W4)(g)	74.5	73.5	74.8
5.	Weight of cement(W5)(g)	12.5	11.5	12.5

Table 4.1 Specific Gravity of Cement

##### 4.1.B. Initial Setting Time Test

SI.NO.	Time in minutes	Pointer reading from bottom
1.	0	0
2.	5	0
3.	10	0
4.	15	0
5.	20	0
6.	25	0
7.	30	0
8.	35	0
9.	40	0
10.	45	0
11.	50	0
12.	55	0.5
13.	60	0.5
14.	65	0.5
15.	70	0.5
16.	75	0.5
17.	80	1.5
18.	85	1.5

19.	90	1.5
20.	95	2.
21.	100	2.0
22.	105	2.5
23.	110	3.0
24.	115	3.5
25.	120	4.5
26.	125	6.0

**4.1.C. Final Setting Time Test**

S.NO	Time in(MIN)	Pointer reading From Top
1.	140	37.5
2.	170	38
3.	200	39
4.	230	40
5.	260	40

*Table 4.3 Final Setting Time*

Needle with annular collar used: - 1mm Square Amount of water added: - 0.85P = 123 ml

**4.1.D. Fineness Modulus Test**

S.No	OBSERVATION	Trial I	Trial II	Trial III
1.	Weight of sample taken	100	100	100
2.	Weight of material retained after sieving	2.8	2.85	2.9
3.	% of Residue left on the sieve on 90 $\mu$	2.8	2.85	2.9

*Table 4.4 Fineness Modulus of Cement Calculations:*

Percentage of residue left on sieve = (weight retained/weight taken) x 100

Fineness Modulus of Cement = 2.85

**Tests for fine aggregate****4.2.A. Specific Gravity Test**

Sl.No	OBSERVATION	Trial I	Trial II	Trial III
1.	Weight of pycnometer W1(g)	450	450	450
2.	Weight of pycnometer + Sand W2(g)	828	846	928
3.	Weight of pycnometer + Sand + Water W3(g)	1484	1486	1538
4.	Weight of pycnometer + Water W4 (g)	1242	1242	1242

*Table 4.5 Specific Gravity of Fine Aggregate***4.2.2.B. Sieve Analysis Test**

Sl.no	IS Sieve Nomm	Wt retained	% of weight retained	% weight Passing	Cumulative % weight retained	Sand Confirming Zone
1.	4.75mm	5	0.5	99.5	0.5	I, II, III, IV
2.	2.36mm	21	2.1	97.4	2.6	II, III, IV
3.	1.18mm	10	1	96.4	3.6	III, IV
4.	600 $\square$	102	10.2	86.2	13.8	III
5.	300 $\square$	580	58	28.2	71.8	II, III, IV
6.	150 $\square$	236	23.6	4.6	95.4	I, II, III, IV
7.	Pan	46	4.6	0	100	-

**4.2.1 Tests for coarse aggregate****4.2.1.A. Specific Gravity Test**

Sl.No.	OBSERVATION	TrialII	TrialIII	TrialIII
1.	Weight of Container(W1)	450	450	450
2.	Weight of Container + Sand(W2)	862	844	812
3.	Weight of Container + Sand + Water(W3)	1512	1498	1478
4.	Weight of Container +Water (W4)	1242	1242	1242

Table 4.7 Specific Gravity of Coarse Aggregate

**4.2.1.B. Fineness modulus Test**

Sl.No.	IS Sieve No mm	Weight retained	% of weight retained	%weight Passing	Cumulative %weight retained
1.	12.5	0	0	100	0
2.	11.2	76	7.6	92.4	7.6
3.	10	206	20.6	71.8	28.2
4.	9.5	195	19.5	52.3	47.7
5.	8	290	29.0	23.3	76.7
6.	6.3	185	18.5	4.8	95.2
7.	5.6	16	1.6	3.2	96.8
8.	4.75	18	1.8	1.4	98.6
9.	Pan	14	1.4	0	100
				Total	550.8

Table 4.8 Fineness modulus for coarse aggregate

**4.2.2 Tests for Fly ash****4.2.4.A Specific Gravity Test**

S.No	DESCRIPTION	TrialII	TrialIII	Trail III
1.	Weight of empty bottle (W1)(g)	26.8	26.8	26.8
2.	Weight of bottle +water(W2)(g)	75	75	75
3.	Weight of bottle + Kerosene (W3) (g)	65.5	65.5	65.5
4.	Weight of bottle+ Cement+ Kerosene (W4) (g)	73	73.5	73.2
5.	Weight of cement(W5)(g)	10	10	10

Table 4.9 Specific Gravity of Flyash

**4.2.4.B Fineness Modulus Test**

S.No	OBSERVATION	TrialII	TrialIII	TrialIII
1.	Weight of sample taken	100	100	100
2.	Weight of material retained after sieving	1.75	1.9	1.8
3.	% of Residue left on the sieve on 90μ	1.75	1.9	1.8

Table 4.10 Fineness Modulus

**Concrete mix design**

Mix design can be define as the process of selecting suitable ingredient so f concrete and determining the rrelative proportions with the object of producing concrete of certain minimum strength and durability as economically as possible finding the proportions, we preferred ACI method for design the mix.

**ACI Method of Design for M30 Concrete Data:**

Compressive Strength required = 30 N/mm<sup>2</sup>

Max size of Aggregate=12.5 mm

Specific Gravity of cement =2.90

Specific Gravity of Fine aggregate = 2.66

Specific Gravity of Coarse aggregate=2.88

Fineness Modulus of fine aggregate = 2.80

**Design:**

1. Required Slump =150–180 mm
2. Max size of Aggregate= 12.5 mm
3. From ACI, Table A1.5.3.3 For slump 150 - 180 mm, 12.5mm CA & Air Entrapped – 2% WaterContent =205kg/m<sup>3</sup>
4. From ACI, Table A 1.5.3.4 (a) For M30,2% Air Entrapped Water Cement ratio (W/C)=0.45
5. Required Cement Content= 205/0.45=455.56 kg/m<sup>3</sup>
6. From ACI, Table A1.5.3.6 For 12.5 mm Aggregate & fineness modulus – 2.8 Volume of Coarse Aggregate per unit volume of Concrete=0.55 Weight of CA =0.55 x1600 =880 kg/m<sup>3</sup>
7. For 12.5mm Aggregate Density of fresh concrete for air entrained concrete=2235 kg/m<sup>3</sup>
8. Weight of Water=205 kg/m<sup>3</sup>  
Weight of Cement = 455.56 kg/m<sup>3</sup>  
Weight of Coarse Aggregate=880kg/m<sup>3</sup>  
Weight of Fine Aggregate=2235– (205 +455.56+880)=694.44kg/m<sup>3</sup>
9. Absolute volume basis:

S.no	Materials	Weight (kg/m <sup>3</sup> )x10-3	Absolute volume(m <sup>3</sup> )
1.	Cement	455.56 / 2.9	0.157
2.	Water	205 / 1	0.205
3.	Coarse aggregate	880 / 2.88	0.306
4.	Air	(2 / 100)x10 <sup>3</sup>	0.02

Total absolute volume=0.687 m<sup>3</sup>

Absolute volume of fine aggregate=(1 – 0.687)=0.312 m<sup>3</sup>

Weight of Fine aggregate =(0.312x2.66)x10<sup>3</sup>=830.89 kg/m<sup>3</sup>

10. Total free surface moisture in Fine Aggregate =(2/100) x 830.89=16.6kg/m<sup>3</sup>

Weight of Fine aggregate in field condition= 830.89+16.6=847.5 kg/m<sup>3</sup>

Coarse Aggregate absorbs 1% water Quantity of water absorbs byCA = (1/100)x880=8.8 kg/m<sup>3</sup>

Weight of Coarse Aggregate in field condition= 880–8.8=871.20kg/m<sup>3</sup>

Weight of Water in field condition =205– (16.6- 8.8)=197.2 kg/m<sup>3</sup>

Cement	FA	CA	W/P
455.56	847.5	871.2	197.2
1	1.86	1.91	0.43

11. Replacing 30% of cement by Fly ash

Weight of Fly ash=0.3x455.56=136.67 kg/m<sup>3</sup>

Weight of Cement = 455.56– 136.67=318.89 kg/m<sup>3</sup>

12. Absolute volume basis:

S.no	Materials	Weight (kg/m <sup>3</sup> )x10-3	Absolute volume(m <sup>3</sup> )
1.	Cement	318.89 / 2.9	0.1099

2.	Fly ash	136.67 / 2.5	0.055
3.	Water	205 / 1	0.205
4.	Coarse aggregate	880 / 2.88	0.306
5.	Air	$(2/100) \times 10^3$	0.02

Total absolute volume =  $0.696\text{m}^3$

Absolute volume of fine aggregate =  $(1 - 0.696) = 0.3048\text{m}^3$

Weight of Fine aggregate =  $(0.3048 \times 2.66) \times 10^3 = 810.77\text{ kg/m}^3$

13. Total free surface moisture in Fine Aggregate =  $(2/100) \times 810.77 = 16.22\text{kg/m}^3$

Weight of Fine aggregate in field condition =  $810.77 + 16.22 = 826.95\text{ kg/m}^3$

Coarse Aggregate absorbs 1% water Quantity of water absorbs by CA =  $(1/100) \times 880 = 8.8\text{ kg/m}^3$

Weight of Coarse Aggregate in field condition =  $880 - 8.8 = 871.20\text{kg/m}^3$

Weight of Water in field condition =  $205 - (16.22 + 8.8) = 197.58\text{ kg/m}^3$

14. Super plastizer–Conplast:1% of Powder material (Cement+Flyash)  $(1/100) \times 455.56 = 4.56\text{ kg/m}^3$

15. Mix Ratio:

Cement	Fly ash	FA	CA	W/P	SP
318.89	136.67	826.98	871.2	197.58	4.5
1	0.43	2.59	2.73	0.43	1%

Table 5.1 Mix Ratio

## Experimental programme

### Program of mix

Experimental test were carried out on series of mixes to evaluate the work ability and strength characteristic based on the following mix ratios.

CC –Cement + F.A + C.A + Water

SCC –CC+Flyash+Super plasticizer

SCC1–SCC + 0.02 % of Glass Fiber

SCC2–SCC + 0.03 % of Glass Fiber

SCC3–SCC + 0.04 % of Glass Fiber

## Result and discussions

Tests were carried out on each mix to evaluate the work ability characteristics. As the results the work ability of nominal concrete is very poor, after the addition of super plasticizer the work ability of concrete increases and it gradually decreases when the addition of Fibers.

### Work ability test results

S.No	Mix	Slump Flow (mm)	T50 Test (Sec)	V– Funnel Test (Sec)	L box Test (h2/ h1)	V– Funnel@ T5 Min(Sec)
1.	SCC	735	3	10	0.9	13
2.	SCC1	720	3	11	0.85	15
3.	SCC2	715	4	12	0.83	15
4.	SCC3	695	4	14	0.8	16

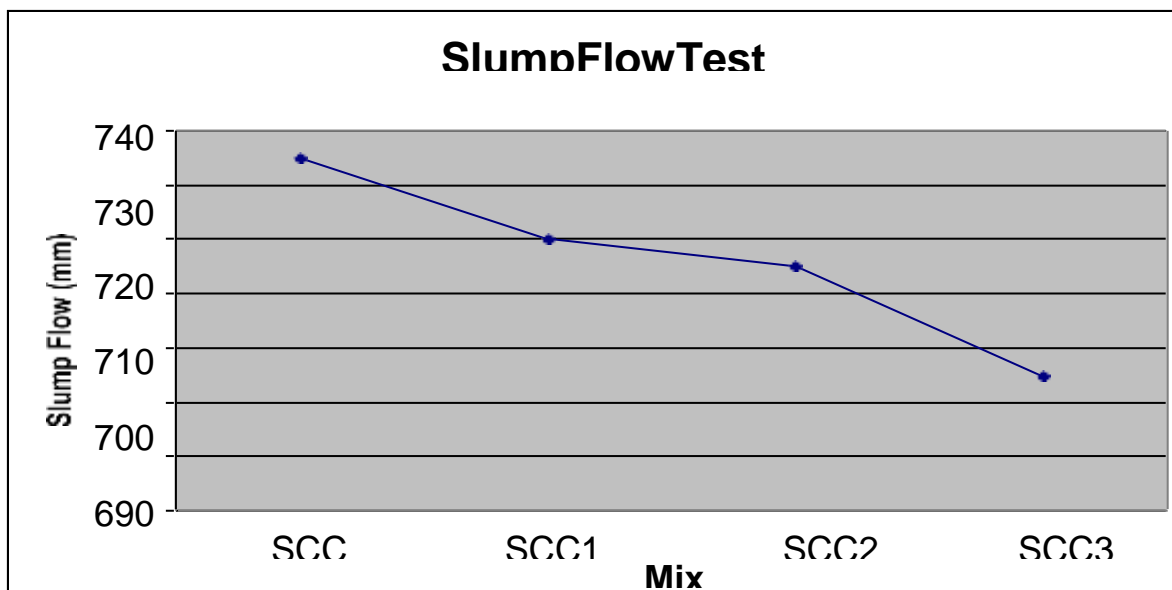


Figure 8.1 Slump Flow Test

## 6.2 Strength test:

### 6.2.1 Compressive strength test:

Compressive strength for different concrete strengths Since concrete is primarily intended to with stand compressive stresses, the determination of compressive strength has received a great deal of attention. Cubes, cylinders, and prisms are three types of compression specimens used to determine compressive strength. Cubes are typically 100 mm or 150 mm on a side and cylinders are 150 mm in diameter and 300 mm high. The prism used in France is 100mmx 100 mmx 500mm. Samples are cast, cured and tested according to the standards prescribed for such testing. If cylinders are used, they must be properly capped prior to testing. This step is not necessary when testing her types of specimens. Different specimens of the same concrete mix report different compressive strengths. Cylinders and prisms with a height or length to transverse dimension ratio of 2 can provide about 75- 85% of the cubic strength of normal strength concrete. It was observed that a maximum compressive strength of 33.92N/mm<sup>2</sup> was obtained with a glass fiber addition of 0.03%. Tensile strength is one of the fundamental and important properties of concrete because concrete is stress-relaxed. Due to it slow tensile strength and brittleness, concrete is usually not expected to with stand direct stress.

MIX	7 Days Compressive Strength (Mpa)				
	%of Glass Fiber	Specimen I	Specimen II	Specimen III	Average
CC	-	28	25.8	27.5	27.09
SCC	-	27.1	26.67	26.2	26.66
SCC1	0.02 %	28	27.1	26.2	27.1
SCC2	0.03 %	28.89	28.4	27.5	28.8
SCC3	0.04 %	26.67	26.72	28	26.96

Table 8.27 days compression test results



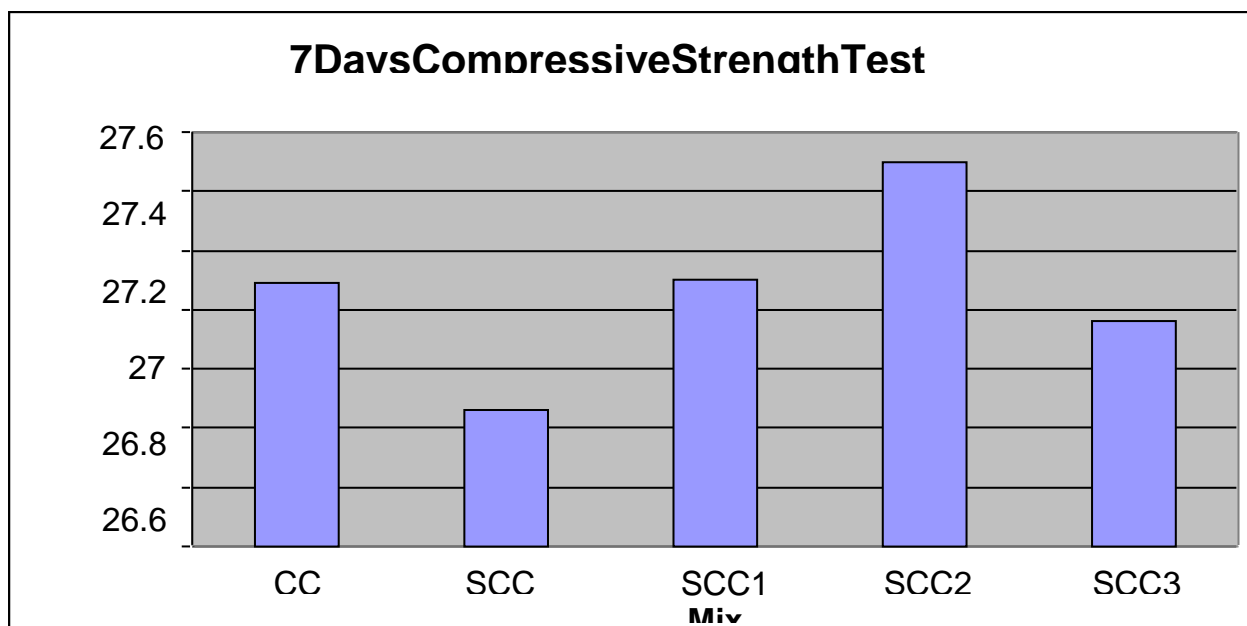


Figure 8.67 Days Compressive Strength Test

MIX	28 Days Compressive Strength (Mpa)				
	% of Glass Fiber	Specimen I	Specimen II	Specimen III	Average
CC	-	32	31.1	33.3	32.1
SCC	-	31.56	33.78	32	32.45
SCC1	0.02 %	32.4	35.1	32.8	33.46
SCC2	0.03 %	32.88	35.56	33.33	33.92
SCC3	0.04 %	31.56	33.33	35	33.3

Table 8.328 days compression test Results

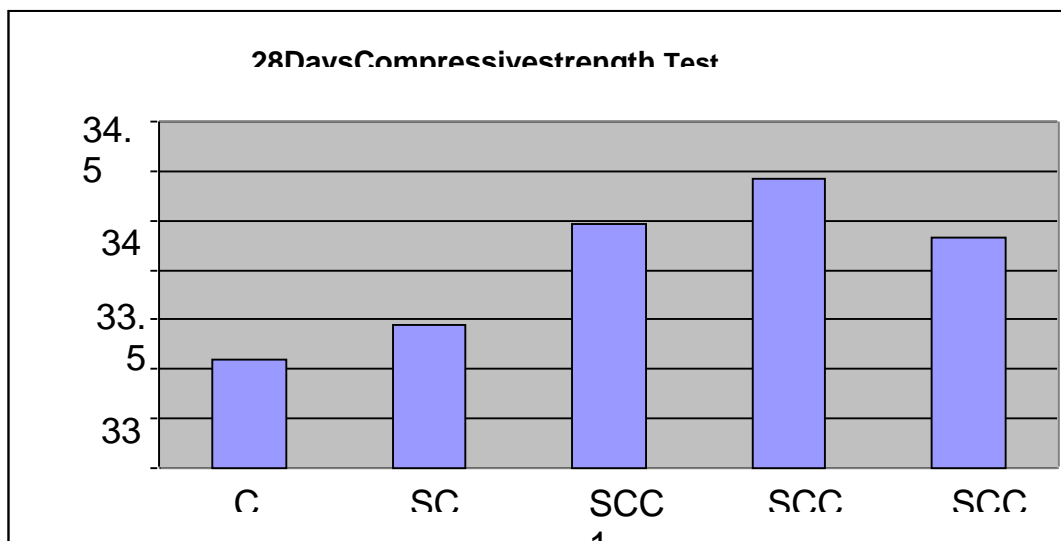


Figure 8.728 Days Compressive Strength Test

#### 4.4 Flexural test

Determination of flexural strength is essential for estimating the loads that can cause concrete members to crack. The tensile strength of concrete is calculated in a bending test as it is measured differently than in a direct tensile test. Therefore, bending strength or modulus of rupture is determined and used as appropriate. His knowledge helps in the design of pavings labs and run ways where bending stress is important. The modulus of rupture was tested on a 150mm x 150mm x 700mm standard specimen with a span of 600mm or a 100mm x 100mm x 500mm with a span of 400mm under symmetrical H is two point loading. Is determined by The modulus of rupture is determined from the moment of failure as  $f_r = M/Z$ . Determining the flexural strength is essential for estimating the loads that can cause concrete members to crack. The tensile strength of concrete is calculated in a bending test as it is measured differently than in a direct tensile test. Therefore, bending strength or modulus of rupture is determined and used as appropriate.

MIX	28DaysFlexural Strength(Mpa)				
	% of Glass Fiber	Specimen I	Specimen II	Specimen III	Average
CC	-	7.6	7.4	6.6	7.2
SCC	-	7.2	8	5.6	6.9
SCC1	0.02 %	6.4	6.8	8.8	7.33
SCC2	0.03 %	7.6	7.2	9.2	8.0
SCC3	0.04 %	8	6.8	8.6	7.8

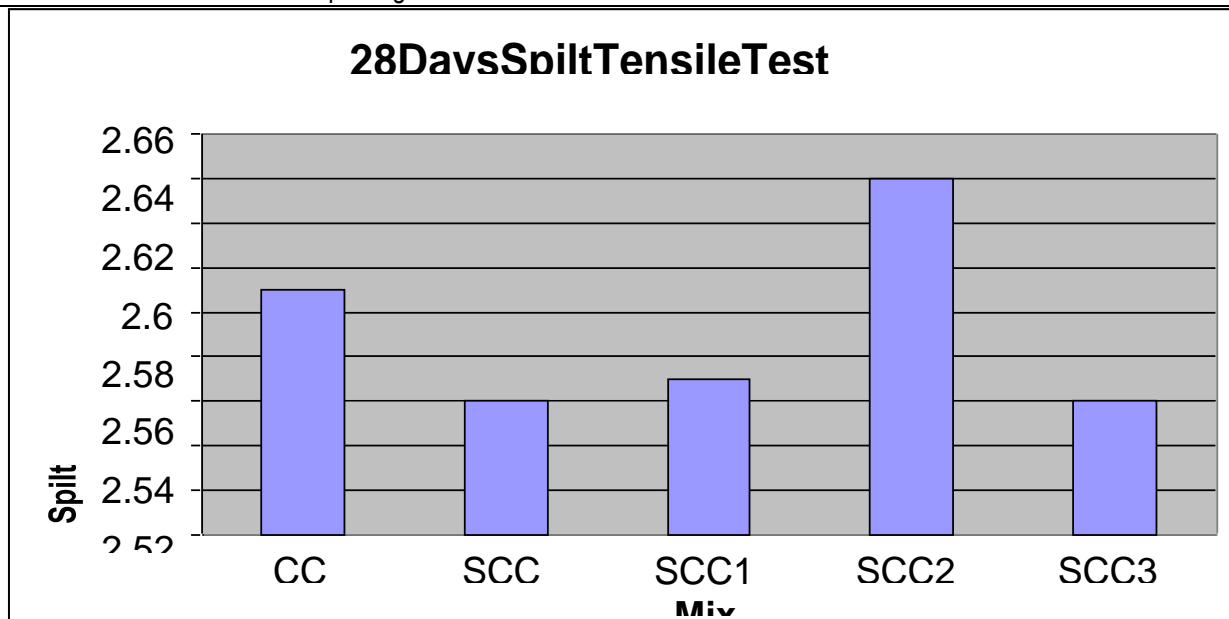
Table 8.4 flexural Test results

#### Split tensile test:

A concrete split test is used to determine the tensile strength of concrete. In general, concrete has low tensile strength values, in this project we will add fibers to increase the tensile strength of concrete, thereby reducing the post-cracking of concrete. After 28 days of curing, remove the wet sample from the water and wipe the water off the surface of the sample. Draw a diameter line on both ends of the sample to ensure they are in the same axial position. Be careful. Set the compression tester to their required range. Hold the strip of plywood on the bottom plate and place the sample. Align the sample so that the line marked on the edge is vertical and centered on the bottom plate. Place another strip of plywood on top of the sample. Lower the top panel so that it touches the plywood strips. Apply load continuously without impact. Note the breaking load.

MIX	28DaysSplitTensileStrength(Mpa)				
	% of Glass Fiber	Specimen I	Specimen II	Specimen III	Average
CC	-	2.12	2.83	2.68	2.54
SCC	-	2.83	2.26	2.59	2.59
SCC1	0.02 %	2.56	2.69	2.41	2.55
SCC2	0.03 %	2.68	2.4	2.83	2.64
SCC3	0.04 %	2.55	1.98	3.12	2.54

Table 8.5 split tensile test results



### V.CONCLUSION

The structural behavior of self-compacting glass fiber reinforced concrete was studied by adding different volumes of glass fiber from 0.02% to 0.04% and using 1% upper plasticizer and 0.8% VMA in cement. Referring to the results of this study, the following conclusions were drawn. The workability of concrete decreases with increasing fiber content. All received concrete mixes are viable, even with reduced values. A maximum compressive strength of 33.92 N/mm<sup>2</sup> was achieved by adding 0.03% fiber to the concrete. The improvement in compressive strength compared to the reference concrete is 5.66%. A maximum split strength of 2.64 N/mm<sup>2</sup> was achieved by adding 0.03% fiber to the concrete. The improvement in split strength compared to the reference concrete is 3.94%. A maximum flexural strength of 8.0 N/mm<sup>2</sup> was achieved by adding 0.03% fibers to the concrete. The improvement in flexural strength compared to the reference concrete is 11.12%. After this experimental investigation, it must be concluded that the incorporation of 0.03% glass fibers in to concrete increased strength by 5.66% in compression, 3.94% in tension and 11.12% in bending after 28 days. Finally, we concluded that 0.03% glass fiber addition to the concrete was optimal and the incorporation of glass fiber should increase the flexural strength relative to the compressive and tensile strength.

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